

Introduction:

➤ Task:

- Design an easy-to-implement and fully differentiable Joint optimization loss for Spherical Image Object Detection.

➤ Challenges:

- Spherical IoU is not differentiable, making it impossible to use as a loss function for box.
- Currently, only independently optimized Ln loss can be used in spherical object detection.

➤ Contributions:

- We explore a new regression loss function based on Gaussian Label Distribution Learning (GLDL) for spherical object detection task. It achieves a trend-level alignment with SphIoU loss and thus naturally improves the model.
- We align the measurement between sample selection and loss regression based on the GLDL, and then construct new dynamic sample selection strategies (GLDL-ATSS) accordingly. GLDL-ATSS can alleviate the drawback of IoU threshold-based strategy (i.e., scale-sample imbalance).
- Extensive experimental results on two datasets and popular spherical image detectors show the effectiveness of our approach.

Proposed Method:

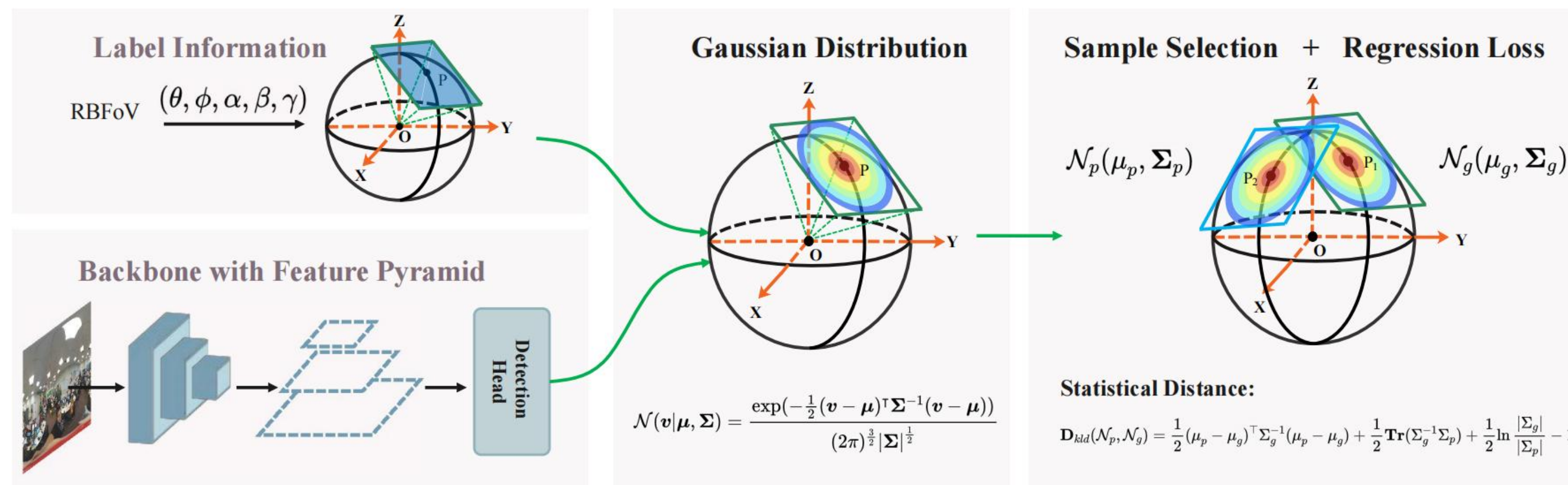
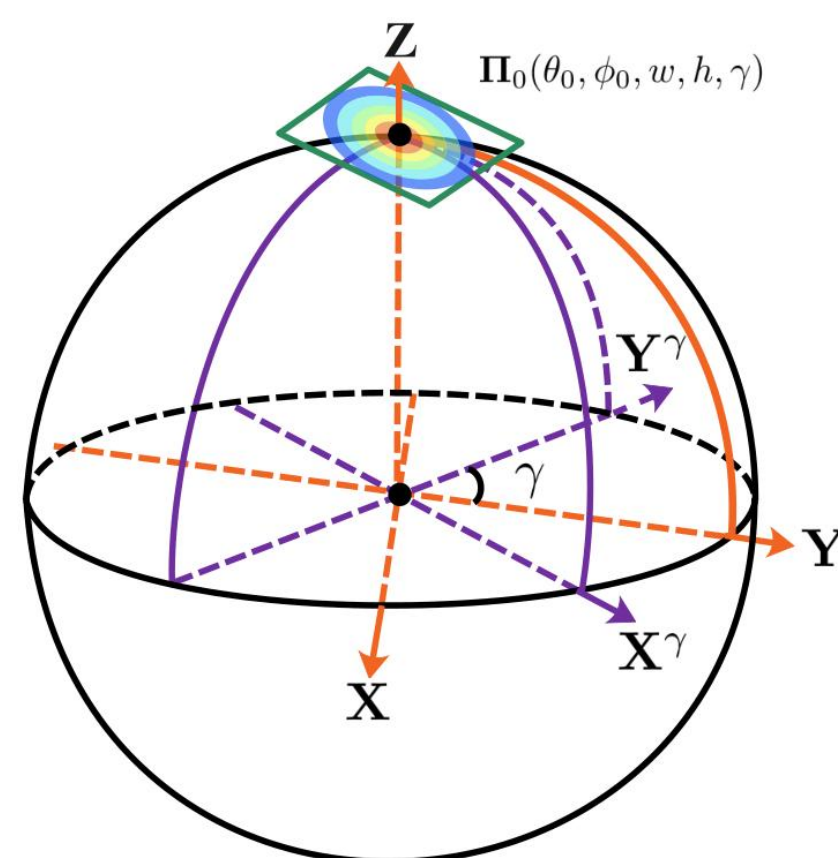
➤ Gaussian Label Distribution Learning

- Firstly, transform the box in polar region to a Gaussian distribution

$$\mu_0 = [\sin(\phi_0) \cos(\theta_0), \sin(\phi_0) \sin(\theta_0), \cos(\phi_0)]$$

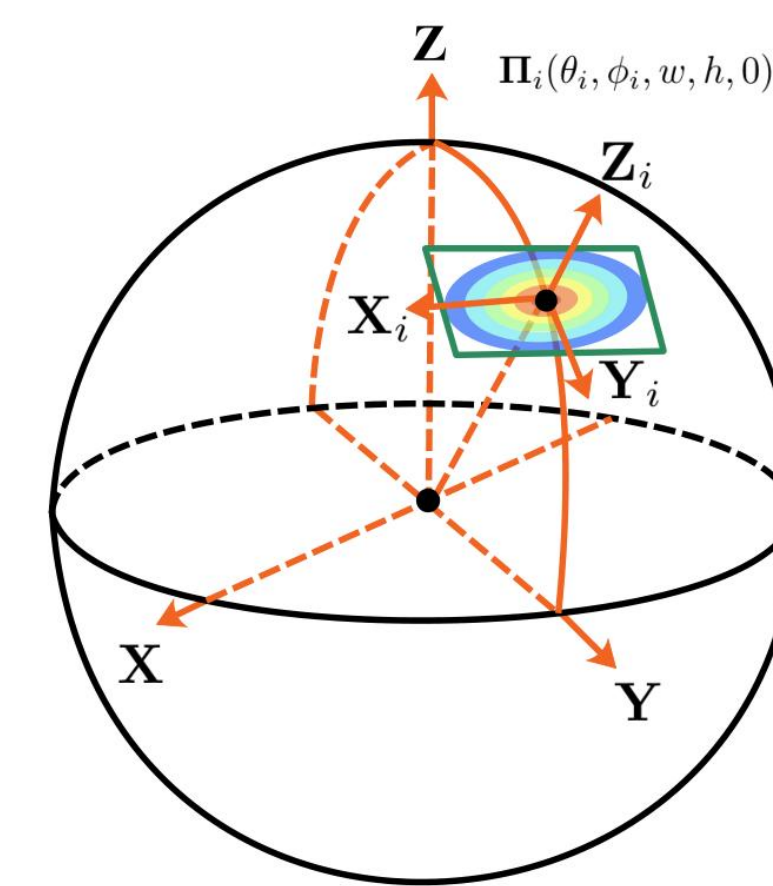
$$\Sigma_0 = \mathbf{R} \mathbf{A} \mathbf{R}^\top,$$

$$\mathbf{R} = \begin{bmatrix} \cos \gamma & -\sin \gamma & 0 \\ \sin \gamma & \cos \gamma & 0 \\ 0 & 0 & 1 \end{bmatrix}, \quad \mathbf{A} = \begin{bmatrix} \frac{w^2}{4} & 0 & 0 \\ 0 & \frac{h^2}{4} & 0 \\ 0 & 0 & 0 \end{bmatrix}$$



- Secondly, establish a new coordinate system

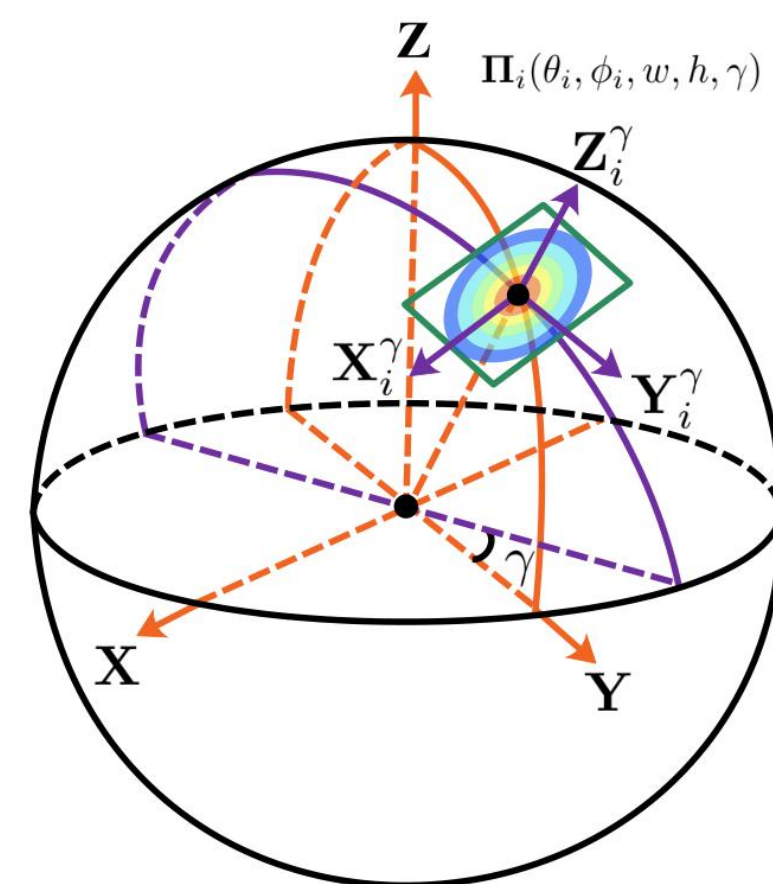
$$\begin{cases} \mathbf{X}_i = [\sin(\theta_i), -\cos(\theta_i), 0]^\top \\ \mathbf{Y}_i = [\cos(\phi_i) \cos(\theta_i), \cos(\phi_i) \sin(\theta_i), -\sin(\phi_i)]^\top \\ \mathbf{Z}_i = [\sin(\phi_i) \cos(\theta_i), \sin(\phi_i) \sin(\theta_i), \cos(\phi_i)]^\top \\ \boldsymbol{\mu}_i = (\sin(\phi_i) \cos(\theta_i), \sin(\phi_i) \sin(\theta_i), \cos(\phi_i)) \\ \boldsymbol{\Sigma}_i = \mathbf{R}(\mathbf{T} \mathbf{\Lambda} \mathbf{T}^\top) \mathbf{R}^\top, \quad \mathbf{T} = [\mathbf{X}_i, \mathbf{Y}_i, \mathbf{Z}_i] \end{cases}$$



- Finally, measure two distributions

$$D_{kl}(\mathcal{N}_p, \mathcal{N}_g) = \frac{1}{2}(\boldsymbol{\mu}_p - \boldsymbol{\mu}_g)^\top \boldsymbol{\Sigma}_g^{-1}(\boldsymbol{\mu}_p - \boldsymbol{\mu}_g) + \frac{1}{2} \text{tr}(\boldsymbol{\Sigma}_g^{-1} \boldsymbol{\Sigma}_p) + \frac{1}{2} \ln \frac{|\boldsymbol{\Sigma}_g|}{|\boldsymbol{\Sigma}_p|} - 1$$

$$\mathcal{L}_{reg} = 1 - \frac{1}{\tau + f(D_{kl})}$$



➤ Sample Selection Based on GLDL-ATSS

$$f(D_{kl}) = \frac{1}{c + D_{kl}(\mathcal{N}_g, \mathcal{N}_p)}$$

$$m_g^i = \frac{1}{N} \sum_{j=1}^N f^{i,j}(D_{kl})$$

$$v_g^i = \sqrt{\frac{1}{N} \sum_{j=1}^N (f^{i,j}(D_{kl}) - m_g^i)^2}$$

$$t_g^i = m_g^i + v_g^i$$



$$\begin{aligned} \text{SphIoU} &= \frac{|A \cap B|}{|A \cup B|} = 0.3 \\ \text{SphIoU} &= \frac{|A \cap C|}{|A \cup C|} = 0.01 \\ \text{GLDL}(A, B) &= 0.51 \\ \text{GLDL}(A, C) &= 0.41 \\ \text{SphIoU} &= \frac{|A \cap B|}{|A \cup B|} = 0.7 \\ \text{SphIoU} &= \frac{|A \cap C|}{|A \cup C|} = 0.6 \\ \text{GLDL}(A, B) &= 0.24 \\ \text{GLDL}(A, C) &= 0.15 \end{aligned}$$

Experiments:

➤ Ablation study of hyper-parameters.

Dataset	$\tau = 1$	$\tau = 2$	$\tau = 3$	$\tau = 4$	$\tau = 5$	baseline
360-Indoor	20.3	20.5	20.4	20.0	19.4	17.6
PANDORA	20.1	20.3	20.1	19.9	19.7	17.2

Dataset	$c = 1$	$c = 2$	$c = 3$	$c = 4$	$c = 5$	baseline
360-Indoor	21.5	21.8	21.7	21.4	21.2	20.1
PANDORA	20.9	21.3	21.2	21.1	22.8	19.6

➤ Ablation study of each component.

Dataset	Backbone	\mathcal{S}_{ss}	\mathcal{L}_{reg}	AP ₅₀
360-Indoor	R-101	\mathcal{S}_{IoU} (Fixed)	\mathcal{L}_{LI}	17.6
	R-101	\mathcal{S}_{IoU} (Fixed)	\mathcal{L}_{GLDL}	20.7 (+3.1)
	R-101	\mathcal{S}_{GLDL} (Fixed)	\mathcal{L}_{GLDL}	22.8 (+5.2)
	R-101	\mathcal{S}_{IoU} (ATSS)	\mathcal{L}_{LI}	20.1
	R-101	\mathcal{S}_{IoU} (ATSS)	\mathcal{L}_{GLDL}	22.3 (+2.2)
	R-101	\mathcal{S}_{GLDL} (ATSS)	\mathcal{L}_{GLDL}	25.0 (+4.9)
PANDORA	R-101	\mathcal{S}_{IoU} (Fixed)	\mathcal{L}_{LI}	17.2
	R-101	\mathcal{S}_{IoU} (Fixed)	\mathcal{L}_{GLDL}	21.4 (+4.2)
	R-101	\mathcal{S}_{GLDL} (Fixed)	\mathcal{L}_{GLDL}	22.7 (+5.5)
	R-101	\mathcal{S}_{IoU} (ATSS)	\mathcal{L}_{LI}	19.6
	R-101	\mathcal{S}_{IoU} (ATSS)	\mathcal{L}_{GLDL}	23.4 (+3.8)
	R-101	\mathcal{S}_{GLDL} (ATSS)	\mathcal{L}_{GLDL}	25.2 (+5.6)

➤ Comparison of the performance of different methods.

Method	Backbone	\mathcal{S}_{ss}		\mathcal{L}_{reg}		360-Indoor			PANDORA		
		\mathcal{S}_{IoU}	\mathcal{S}_{GLDL}	\mathcal{L}_{LI}	\mathcal{L}_{GLDL}	AP	AP ₅₀	AP ₇₅	AP	AP ₅₀	AP ₇₅
Multi-Kernel [26]	R-101	✓		✓		4.7	11.1	2.8	4.2	10.8	2.2
	R-101	✓		✓	✓	7.2(+2.5)	14.2(+4.1)	5.4(+2.4)	7.8(+3.6)	15.6(+4.8)	4.3(+2.1)
	R-101		✓	✓	✓	6.8(+2.1)	13.9(+2.8)	4.7(+1.9)	6.2(+2.0)	14.5(+3.7)	3.9(+1.7)
	R-101		✓	✓	✓	9.3(+4.6)	17.2(+6.1)	6.6(+3.8)	10.2(+6.0)	17.6(+6.8)	6.9(+4.4)
Sphere-SSD [4]	R-101	✓		✓		2.9	7.8	1.4	2.3	7.7	1.5
	R-101	✓		✓	✓	5.6(+2.7)	10.8(+3.0)	4.2(+2.8)	5.9(+3.6)	12.3(+4.6)	4.9(+3.4)
	R-101		✓	✓	✓	4.9(+2.0)	10.2(+2.4)	3.7(+2.3)	4.1(+1.8)	9.8(+2.1)	3.2(+1.7)
	R-101		✓	✓	✓	7.8(+4.9)	12.6(+4.8)	5.4(+3.4)	8.0(+5.7)	13.8(+6.1)	6.8(+5.3)
Reprojection R-CNN [36]	R-101	✓		✓		5.0	15.3	1.9	4.2	14.7	1.8
	R-101	✓		✓	✓	7.5(+2.5)	18.2(+2.9)	3.8(+1.9)	7.9(+3.7)	18.7(+4.0)	4.5(+2.7)
	R-101		✓	✓	✓	7.1(+2.1)	17.8(+2.5)	3.2(+1.3)	6.8(+2.6)	17.4(+2.7)	3.0(+1.2)
Sphere-CenterNet [5]	R-101		✓	✓	✓	10.0	24.8	6.0	-	-	-
	R-101		✓	✓	✓	11.2(+1.1)	26.1(+1.3)	7.4(+1.4)	-	-	-
R-CenterNet [27]	R-101			✓		-	-	-	7.3	22.7	2.6
	R-101			✓	✓	-	-	-	8.7(+1.4)	24.3(+1.6)	4.5(+1.9)